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Transmitted herewith for filing is the Patent Application of:

Inventors: Mark N. WEGMAN et al.

For: DOMINANT EDGE IDENTIFICATION FOR EFFICIENT PARTITION AND DISTRIBUTION  
Enclosed are:

X 7 Sheets of Informal Drawings.

       An assignment of the invention to International Business Machines Corporation, Armonk, New York 10504.

       A certified copy of a                      application.

X Declaration and Power of Attorney is attached to the application.

       Associate Power of Attorney.

       Information Disclosure Statement with form PTO-1449 with references attached.

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Respectfully submitted,

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# **DOMINANT EDGE IDENTIFICATION FOR EFFICIENT PARTITION AND DISTRIBUTION**

## **DESCRIPTION**

### **RELATED APPLICATION**

5           The present application is related to U.S. Patent Application No. 09/\_\_\_\_\_  
(Attorney Docket No. YOR9-2000-0293-US1) entitled "INDEPENDENT NET TASK  
IDENTIFICATION FOR EFFICIENT PARTITION AND DISTRIBUTION" to  
Kimelman et al.; U.S. Patent Application No. 09/\_\_\_\_\_  
10           (Attorney Docket No. YOR9-2000-0464-US1) entitled "MACHINE CUT TASK IDENTIFICATION FOR  
EFFICIENT PARTITION AND DISTRIBUTION" to Rajan et al.; and U.S. Patent  
Application No. 09/\_\_\_\_\_  
15           (Attorney Docket No. YOR9-2000-0465-US1) entitled  
"NET ZEROING FOR EFFICIENT PARTITION AND DISTRIBUTION" to Roth et al.,  
all filed coincident herewith and assigned to the assignee of the present invention.

### **BACKGROUND OF THE INVENTION**

#### *Field of the Invention*

15           The present invention generally relates to distributed processing and more  
particularly, the present invention relates to efficiently assigning tasks across multiple  
computers for distributed processing.

### *Background Description*

Any large, multifaceted project, such as a complex computer program, may be segmented into multiple smaller manageable tasks. The tasks then may be distributed amongst a group of individuals for independent completion, e.g., an engineering design project, distributed processing or, the layout of a complex electrical circuit such as a microprocessor. Ideally, the tasks are matched with the skills of the assigned individual and each task is completed with the same effort level as every other task. However, with such an ideal matched task assignment, intertask communication can become a bottleneck to project execution and completion. Thus, to minimize this potential bottleneck, it is important to cluster together individual tasks having the highest level of communication with each other. So, for example, in distributing eight equivalent tasks to pairs of individuals at four locations, (e.g., eight design engineers in four rooms) optimally, pairs of objects or tasks with the highest communication rate with each other are assigned to individual pairs at each of the four locations.

Many state of the art computer applications are, by nature, distributed applications. End-users sit at desktop workstations or employ palmtop information appliances on the run, while the data they need to access resides on distant data servers, perhaps separated from these end-users by a number of network tiers. Transaction processing applications manipulate data spread across multiple servers. Scheduling applications are run on a number of machines that are spread across the companies of a supply chain, etc.

When a large computer program is partitioned or segmented into modular components and the segmented components are distributed over two or more machines, for the above mentioned reasons, component placement can have a significant impact on program performance. Therefore, efficiently managing distributed programs is a major

challenge, especially when components are distributed over a network of remotely connected computers. Further, existing distributed processing management software is based on the assumption that the program installer can best decide how to partition the program and where to assign various program components. However, experience has shown that programmers often do a poor job of partitioning and component assignment.

So, a fundamental problem facing distributed application developers is application partitioning and component or object placement. Since communication cost may be the dominant factor constraining the performance of a distributed program, minimizing inter-system communication is one segmentation and placement objective. Especially when placement involves three or more machines, prior art placement solutions can quickly become unusable, i.e., what is known as NP-hard. Consequently, for technologies such as large application frameworks and code generators that are prevalent in object-oriented programming, programmers currently have little hope of determining effective object placement without some form of automated assistance. En masse inheritance from towering class hierarchies, and generation of expansive object structures leaves programmers with little chance of success in deciding on effective partitioning. This is particularly true since current placement decisions are based solely on the classes that are written to specialize the framework or to augment the generated application.

Furthermore, factors such as fine object granularity, the dynamic nature of object-based systems, object caching, object replication, ubiquitous availability of surrogate system objects on every machine, the use of factory and command patterns, etc., all make partitioning in an object-oriented domain even more difficult. In particular, for conventional graph-based approaches to partitioning distributed applications, fine-grained object structuring leads to enormous graphs that may render these partitioning approaches impractical.

Finally, although there has been significant progress in developing middleware and in providing mechanisms that permit objects to inter-operate across language and machine boundaries, there continues to be little to help programmers decide object-system placement. Using state of the art management systems, it is relatively straightforward for objects on one machine to invoke methods on objects on another machine as part of a distributed application. However, these state of the art systems provide no help in determining which objects should be placed on which machine in order to achieve acceptable performance. Consequently, the initial performance of distributed object applications often is terribly disappointing. Improving on this initial placement performance is a difficult and time-consuming task.

Accordingly, there is a need for a way of automatically determining the optimal program segmentation and placement of distributed processing components to minimize communication between participating distributed processing machines.

### SUMMARY OF THE INVENTION

It is therefore a purpose of the present invention to improve distributed processing performance;

It is another purpose of the present invention to minimize communication between distributed processing machines;

It is yet another purpose of the invention to improve object placement in distributed processing applications;

It is yet another purpose of the invention to determine automatically how objects should best be distributed in distributed processing applications

it is yet another purpose of the invention to minimize communication between objects distributed amongst multiple computers in distributed processing applications.

The present invention is a task management system, method and computer program product for determining optimal placement of task components on multiple machines for task execution, particularly for placing program components on multiple computers for distributed processing. First, a communication graph is generated representative of the computer program with each program unit (e.g., an object) represented as a node in the graph. Nodes are connected to other nodes by edges representative of communication between connected nodes. A weight is applied to each edge, the weight being a measure of the level of communication between the connected edges. Terminal nodes representative of the multiple computers are attached to the communication graph. Then, dominant edges are identified within the communication graph. For any non-terminal node, a connected edge is dominant if it is at least as heavy (its weight is greater than or equal to) as the sum of the remaining non-terminal edges and the heaviest of the remaining terminal edges. The min cut for the communication graph need not include any dominant edges and so, dominant edges are removed from consideration for the final min cut solution. Finally, program components which may be a single program unit or an aggregate of units are placed on computers according to the communication graph min cut solution.

## BRIEF DESCRIPTION OF THE DRAWINGS

YOR9-2000-0466-US1

The foregoing and other objects, aspects and advantages will be better understood from the following detailed preferred embodiment description with reference to the drawings, in which:

Figure 1 shows an example of a flow diagram of the preferred embodiment of the present invention wherein a program is segmented, initially, and initial segments are distributed to and executed on multiple computers;

Figures 2A-C show an example of a communication graph;

Figure 3 is a flow diagram of the optimization steps for determining an optimum distribution of program components;

Figure 4 shows an example of a portion of a communication graph reducible by the preferred embodiment Dominant Edge method;

Figure 5 is an example of the steps of identifying dominant edges;

Figure 6 is an example of the steps in contracting a dominant edge.

## **DETAILED DESCRIPTION OF PREFERRED EMBODIMENTS OF THE INVENTION**

As referred to herein, a communication graph is a graphical representation of a multifaceted task such as a computer program. Each facet of the task is an independent task or object that is represented as a node and communication between tasks or nodes is represented by a line (referred to as an edge) between respective communicating nodes. Participating individuals (individuals receiving and executing distributed tasks) are referred to as terminal nodes or machine nodes. A net is a collection of nodes connected together by edges. Two nets are independent if none of the non-terminal nodes of one net shares an edge with a non-terminal node of the other. Thus, for example, a communication graph of a computer program might include a node for each program object and edges would be between communicating objects, with edges not being included between objects not

communicating with each other. In addition, a weight indicative of the level of communication between the nodes may be assigned to each edge. Graphical representation and modeling of computer programs is well known in the art.

Referring now to the drawings, and more particularly, Figure 1 is an example of a flow diagram 100 of the preferred embodiment of the present invention wherein a program is segmented, initially, and initial segments are distributed to and executed on multiple computers. First, in step 102 the communication patterns of a program are analyzed to form a communication graph. Then, in step 104, the traces of the communication graph are analyzed, and an initial partition is determined. In step 106, the partition is optimized for minimum interpartition communication. In step 108, the individual objects are distributed amongst participants for execution according to the optimize partition of step 106.

A component refers to an independent unit of a running program that may be assigned to any participating individual, e.g., computers executing objects of a distributed program. Thus, a component may refer to an instance of an object in an object oriented program, a unit of a program such as Java Bean or Enterprise Java Bean or, a larger collection of program units or components that may be clustered together intentionally and placed on a single participating machine. Further, a program is segmented or partitioned into segments that each may be a single component or a collection of components. After segmenting, analyzing the segments and assigning each of segments or components to one of the multiple participating machines or computers according to the present invention, the final machine assignment is the optimal assignment.

Thus, a typical communication graph includes multiple nodes representative of components with weighted edges between communicating nodes. Determining



communication between components during program execution may be done using a typical well known tool available for such determination. Appropriate communication determination tools include, for example, Jinsight, for Java applications that run on a single JVM, the Object Level Tracing (OLT) tool, for WebSphere applications or, the monitoring tool in Visual Age Generator.

Figures 2A-C show an example of a communication graph of a net 110 that includes multiple nodes 112, 114, 116, 118, 120 and 122. Each node 112, 114, 116, 118, 120 and 122 represents a program component connected to communication edges 124, 126, 128, 130, 132, 134, 136 and 138 to form the net 110. Adjacent nodes are nodes that share a common edge, e.g., nodes 114 and 122 share edge 126. Each edge 124, 126, 128, 130, 132, 134, 136 and 138 has been assigned a weight proportional to, for example, the number of messages between the adjacent components.

In Figure 2B, Machine nodes 140, 142 and 144 representative of each participating machine (three in this example) are shown connected by edges 146, 148, 150. Initially, a node 112, 114, 116, 118, 120 and 122 may be placed on a machine 140, 142, 144 by adding an edge 146, 148, 150 with infinite weight (indicating constant communication) between the node and the machine. Typically, initial assignment places nodes with specific functions (e.g., database management) on a machine suited for that function. After the initial placement assigning some nodes 112, 114 and 122 to machines 140, 142, 144, other nodes 116, 118, 120 are assigned to machines 140, 142, 144, if they communicate heavily with a node 112, 114, 122 already assigned to that machine 140, 142, 144. Additional assignment is effected by selectively collapsing edges, combining the nodes on either end of the collapsed edge and re-assigning edges that were attached to one of the two former adjacent nodes to the combined node. When assignment is complete, all of the nodes 112, 114, 116, 118, 120 and 122 will have been placed on one of the machines at terminal

nodes 140, 142, 144 and the final communication graph may be represented as terminal nodes 140, 142, 144 connected together by communication edges.

For this subsequent assignment, the graph is segmented by cutting edges and assigning nodes to machines as represented by 152, 154 and 156 in Figure 2C to achieve what is known in the art as a minimal cut set or min cut set. A cut set is a set of edges that, if removed, eliminate every path between a pair of terminal nodes (machine nodes) in the graph. A min cut set is a cut set wherein the sum of the weights of the cut set edges is minimum. While there may be more than one min cut set, the sum is identical for all min cut sets. A min cut may be represented as a line intersecting the edges of a min cut set. So, in the example of Fig. 2C, the sum of the weights of edges 124, 126, 128, 132 and 138 is 2090, which is cost of the cut and is representative of the total number of messages that would be sent between machines at terminal nodes 140, 142, 144 with this particular placement. The min cut identifies the optimum component placement with respect to component communication. While selecting a min cut set may be relatively easy for this simple example, it is known to increase in difficulty exponentially with the number of nodes in the graph.

Figure 3 is a flow diagram 160 of the optimization steps for determining an optimum distribution of program components to individual participating computers according to a preferred embodiment of the present invention. First, in step 162, an initial communication graph is generated for the program. Then, in step 164 machine nodes are added to the communication graph. As noted above, certain types of components are designated, naturally, for specific host machine types, e.g., graphics components are designated for clients with graphics capability or, server components designated for a data base server. After assigning these host specific components, in step 168 independent nets are identified and the communication graph is partitioned into the identified independent

nets as described in U.S. Patent Application No. 09/\_\_\_\_\_ (Attorney Docket No. YOR9-2000-0293-US1) entitled "INDEPENDENT NET TASK IDENTIFICATION FOR EFFICIENT PARTITION AND DISTRIBUTION" to Kimelman et al., assigned to the assignee of the present invention and incorporated herein by reference. In step 170 a min cut is identified for each of the independent nets, using the preferred embodiment Dominant Edge reduction method to reduce the independent nets and identify the min cut according to the present invention described hereinbelow. The min cuts for all of the independent nets are the min cut for the whole communication graph.

Figure 4 shows an example of a portion of a communication graph 180 reducible by the preferred embodiment Dominant Edge method of the present invention. In this example, the graph portion 180 includes four (4) non-terminal nodes 182, 184, 186 and 188 and four terminal nodes 190, 192, 194 and 196. Node 182 is connected, respectively, to non-terminal nodes 184, 186 and 188 by edges 198, 200 and 202, referred to as non-terminal edges, and to terminal nodes 190, 192, 194 and 196 by edges 204, 206, 208 and 210, referred to as terminal edges.

According to the present invention, for any non-terminal node a connected edge is dominant if it is at least as heavy (its weight is greater than or equal to) as the sum of the remaining non-terminal edges and the heaviest of the remaining terminal edges. Further, every communication graph contains a min cut solution that does not include dominant edges. Thus, dominant edges may be contracted. So, for node 182 in this example, edge 200 is the heaviest edge (30) and edge 204 is the heaviest terminal edge (20). The sum of the remaining non-terminal edges 198 and 202 and edge 204 is 25 (2 + 3 + 20) which is less than edge 200. Thus, non terminal edge 200 is a dominant edge and may be collapsed combining nodes 182 and 186 to reduce the graph and, therefore, simplify the min cut solution somewhat.

Figure 5 is an example of the steps 220 of identifying dominant edges according to the preferred embodiment of the present invention. First, in step 222, non-terminal nodes adjacent to at least two or more terminal nodes are identified. In step 224 the heaviest edge is identified for each node. Then, in step 226, nodes are identified that potentially are connected to a dominant edge as those nodes that, when excluding the heaviest edge, are still adjacent to at least two or more terminal nodes. In step 228, again excluding the heaviest edge, the weight of the heaviest terminal edge is added to the sum of the weights of the non-terminal edges. In step 230, that sum is compared against the weight of the heaviest edge. If the heaviest edge is heavier than the sum, then, the heaviest edge is a dominant edge and, as such, is not required for inclusion in a min cut solution. Otherwise, the heaviest edge is not a dominant edge 232. Each dominant edge is collapsed in step 234.

In other words, for any non-terminal node that is adjacent to three (3) or more terminals nodes, if the heaviest of the edges incident to the given non-terminal node is a terminal edge connecting to a terminal node; then, if the weight of that heaviest edge is greater than or equal to the sum of the weights of all non-terminal edges at the non-terminal node plus the weight of the second-heaviest terminal edge, then that heaviest edge satisfies the condition and is a dominant edge. Likewise, if the non-terminal node is adjacent to two or more terminals nodes, and if the heaviest of the edges incident to the given non-terminal node is a non-terminal edge; then, if that heaviest edge has weight greater than or equal to the sum of the weights of all of the remaining non-terminal edges plus the weight of the heaviest terminal edge, then that heaviest edge satisfies the condition and so, is a dominant edge. A dominant edge is not part of the (only) multiway minimum cut of the graph, and as such, may be contracted or collapsed.

Figure 6 is an example of the steps in contracting a dominant edge 232. First in step 2320 the two nodes connected by the dominant edge are merged, resulting in a single merged node that includes the components of both original nodes. Then, in step 2322 the dominant edge is discarded. Finally, in step 2324 any “parallel” edge groups (edges connecting the merged node to the same adjacent node) resulting from the merger are replaced with a single edge with its weight equal to the sum of parallel edge weights. Thus, as a result of contracting dominant edges, the graph has been reduced wherein a min cut solution may be found with less effort.

In the preferred embodiment, the min cut step 170 is an iterative process, wherein independent nets are reduced using, when necessary, the Dominant Edge identification steps described herein in combination with the Machine Cut method of U.S. Patent Application No. 09/\_\_\_\_\_ (Attorney Docket No. YOR9-2000-0464-US1) entitled “MACHINE CUT TASK IDENTIFICATION FOR EFFICIENT PARTITION AND DISTRIBUTION” to Rajan et al., and the Net Zeroing method of U.S. Patent Application No. 09/\_\_\_\_\_ (Attorney Docket No. YOR9-2000-0465-US1) entitled “NET ZEROING FOR EFFICIENT PARTITION AND DISTRIBUTION” to Roth et al., filed coincident herewith, assigned to the assignee of the present invention and incorporated herein by reference. Further, as independent nets are reduced, those reduced nets are further checked as in step 168 above to determine if they may be divided into simpler independent nets. Then, the Dominant Edge method of the preferred embodiment is applied to those simpler independent nets. To reach a solution more quickly, on each subsequent pass, only nodes and edges of a subgraph that were adjacent to areas reduced previously are rechecked. Thus, the communication graph is simplified by eliminating dominant edges to reach a min cut solution much quicker and much more efficiently than with prior art methods.

The reduction method of the preferred embodiment reduces the number of independent components in the communication graph of a complex program. In the best case, an appropriate allocation of every component in the program is provided. However, even when best case is not achieved, the preferred embodiment method may be combined  
5 with other algorithms and heuristics such as the branch and bound algorithm or the Kernighan-Lin heuristic to significantly enhance program performance. Experimentally, the present invention has been applied to communication graphs of components in several programs with results that show significant program allocation improvement, both in the quality of the final solution obtained and in the speed in reaching the result.

10 Although the preferred embodiments are described hereinabove with respect to distributed processing, it is intended that the present invention may be applied to any multi-task project without departing from the spirit or scope of the invention. Thus, for example, the task partitioning and distribution method of the present invention may be applied to VLSI design layout and floor planning, network reliability determination, web  
15 pages information relationship identification, and "divide and conquer" combinatorial problem solution approaches, e.g., "the Traveling Salesman Problem."

While the invention has been described in terms of preferred embodiments, those skilled in the art will recognize that the invention can be practiced with modification within the spirit and scope of the appended claims.

## CLAIMS

What is claimed is:

1. A task management method for determining optimal placement of task components, said method comprising:

5 a) generating a communication graph representative of a task, task components represented as nodes of said communication graph and edges connecting ones of said nodes, said edges representing communication between connected nodes and being weighted proportional to communication between connected nodes;

b) identifying dominant edges within said communication graph;

10 c) determining a min cut solution for said communication graph, dominant edges being excluded from determined min cut solutions; and

d) placing task components responsive to said min cut solution.

2. A task management method as in claim 1, after the step (a) of generating a communication graph, further comprising the steps of:

15 a1) assigning terminal nodes, task components being placed on said terminal nodes in the task placing step (d); and

a2) identifying independent nets in said communication graph, each of said independent nets being connected between a plurality of said terminal nodes.

3. A task management method as in claim 2, wherein the step (b) of identifying dominant edges comprises the steps of:

20 i) identifying non-terminal nodes adjacent to at least two terminal nodes;

ii) identifying the heaviest edge among edges attached to said each identified node;

iii) identifying nodes that, when excluding the respective heaviest edge, are still adjacent to at least two or more terminal nodes;

iv) summing weights of selected edges about each of said nodes identified in step iii), excluding the respective heaviest edge, by adding the weight of the heaviest remaining terminal edge and the weights of the non-terminal edges; and

v) for each said sum, comparing the weight of the respective heaviest edge with said sum, the weight of dominant edges exceeding respective ones of the sums.

4. A task management method as in claim 3, wherein the step (c) of determining a min cut solution includes reducing the set of independent nets by selectively collapsing dominant edges responsive to said comparison.

5. A task management method as in claim 4, wherein dominant edges are selectively collapsed comprising the steps of:

i) merging nodes at opposite end of each selected heaviest edge to form a single merged node including the components of both original nodes;

ii) discarding the selected heaviest edge; and

iii) replacing groups of parallel edges with a single edge having a weight equal to the sum of parallel edge weights.

6. A task management method as in claim 5, wherein the step (c) of determining a min cut solution comprises the steps of:

i) identifying independent nets in said reduced nets;

ii) identifying and collapsing dominant edges in said identified independent nets, said independent nets being further reduced; and

iii) repeating steps (i) - (ii) until a min cut solution has been found.



7. A task management method as in claim 6, wherein each said task component is a unit of the computer program.

8. A task management method as in claim 7, wherein said each computer program unit is an instance of an object in an object oriented program

5 9. A task management method as in claim 7, wherein in step (d) computer program units are placed on computers, computer program units being placed on a common computer being combined into a single component.

10 10. A task management method as in claim 6 wherein said task is integrated circuit chip functional element placement and said task components are logic elements, said logic elements being placed on an integrated circuit chip in placement step (d).

11. A distributed processing system for determining optimal placement of computer program components on multiple computers, said distributed processing system comprising:

15 means for generating a communication graph of nodes interconnected by edges and representative of a computer program, computers executing said computer program being represented as terminal nodes, computer program components being represented as non-terminal nodes, said edges representing communication between connected nodes and being weighted proportional to communication between connected nodes;

means for identifying dominant edges within said communication graph;

20 means for determining a min cut solution for said communication graph, dominant edges being excluded from determined min cut solutions; and

means for placing program components on ones of said computers responsive to said determined min cut solution; and

said computer program being executed by said computers.

12. A distributed processing system as in claim 11, further comprising:

5 means for identifying independent nets connected between a plurality of said terminal nodes.

13. A distributed processing system as in claim 12, further comprising:

means for collapsing identified dominant edges.

14. A distributed processing system as in claim 13, wherein the means for identifying dominant edges comprises:

means for identifying non-terminal nodes adjacent to at least two terminal nodes;

means for identifying the heaviest edge among edges attached to said each identified node;

15 summing means for adding the weight of the heaviest remaining terminal edge and the weights of the non-terminal edges while excluding the identified heaviest edge; and

means for comparing the weight of the identified heaviest edge with a sum from said summing means, the weight of any identified heaviest edge exceeding said sum indicating that said identified heaviest edge is a dominant edge.

15. A distributed processing system as in claim 14, the means for collapsing dominant edges further comprising:

20 means for merging nodes on either end of a dominant edge and discarding said dominant edge; and

means for replacing pairs of parallel edges attached to said merged node with a single edge.

16. A distributed processing system as in claim 15, wherein each said program component is a unit of the computer program.

17. A distributed processing system as in claim 16, wherein said each program unit is an instance of an object in an object oriented program

18. A computer program product for determining optimal placement of functional components, said computer program product comprising a computer usable medium having computer readable program code thereon, said computer readable program code comprising:

computer readable program code means for generating a communication graph of nodes interconnected by edges and representative of a function, said nodes including a plurality of terminal nodes, functional components being represented as non-terminal nodes, said edges representing communication between connected nodes and being weighted proportional to communication between connected nodes;

computer readable program code means for identifying dominant edges within said communication graph;

computer readable program code means for determining a min cut solution for said communication graph, dominant edges being excluded from determined min cut solutions; and

computer readable program code means for placing functional components on said terminal nodes responsive to said determined min cut solutions.

19. A computer program product as in claim 18, further comprising:  
computer readable program code means for identifying independent nets connected  
between a plurality of said terminal nodes.

20. A computer program product as in claim 19, further comprising:  
computer readable program code means for collapsing identified dominant edges.

21. A computer program product as in claim 19, wherein the computer readable  
program code means for identifying dominant edges comprises:

computer readable program code means for identifying non-terminal nodes  
adjacent to at least two terminal nodes;

computer readable program code means for identifying the heaviest edge among  
edges attached to said identified node;

computer readable program code means for summing the weight of the heaviest  
remaining terminal edge with the weights of the non-terminal edges while excluding the  
identified heaviest edge; and

computer readable program code means for comparing the weight of the identified  
heaviest edge with the sum, the weight of any identified heaviest edge exceeding said sum  
indicating that said identified heaviest edge is a dominant edge.

22. A computer program product as in claim 21, the means for collapsing dominant  
edges further comprising:

computer readable program code means for merging nodes on either end of a  
dominant edge and discarding said dominant edge; and

computer readable program code means for replacing pairs of parallel edges  
attached to said merged node with a single edge.

23. A computer program product as in claim 22, wherein said function is a computer program and each said functional component is a unit of the computer program.

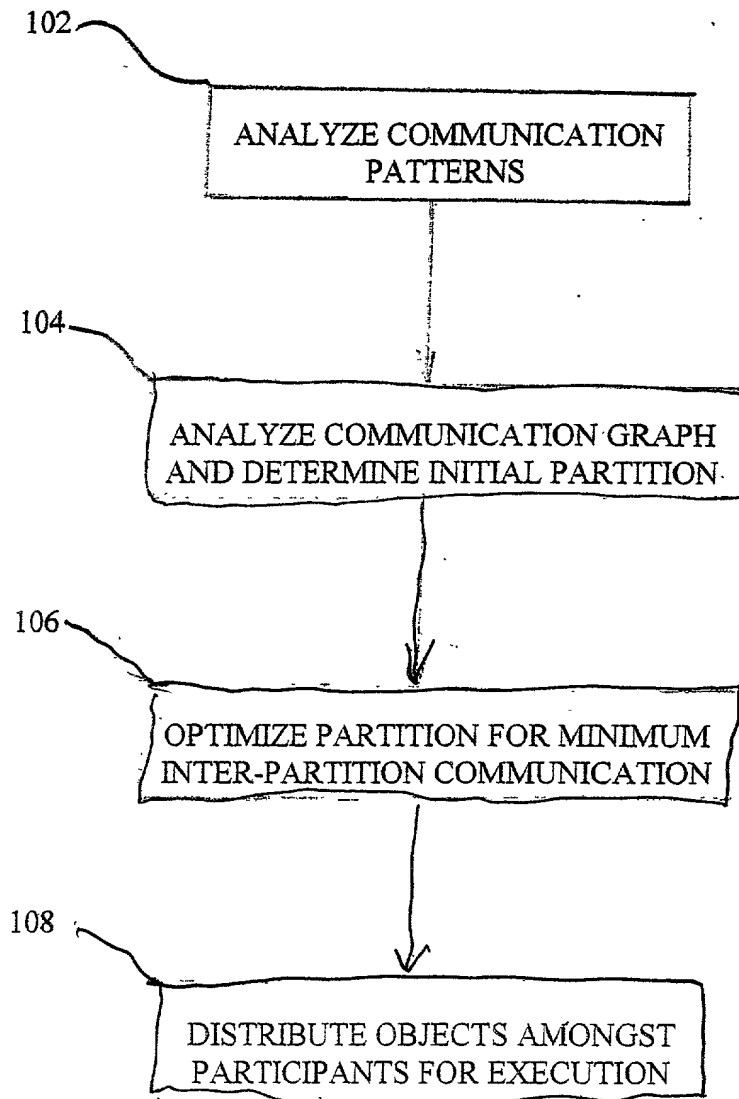
24. A computer program product as in claim 23, wherein each said program unit is an instance of an object in an object oriented program.

5 25. A computer program product as in claim 22 wherein said function is an integrated circuit and said functional components are logic elements.

# **DOMINANT EDGE IDENTIFICATION FOR EFFICIENT PARTITION AND DISTRIBUTION**

## **ABSTRACT OF THE INVENTION**

5           A task management system, method and computer program product for  
determining optimal placement of task components on multiple machines for task  
execution, particularly for placing program components on multiple computers for  
distributed processing. First, a communication graph is generated representative of the  
computer program with each program unit (e.g., an object) represented as a node in the  
10 graph. Nodes are connected to other nodes by edges representative of communication  
between connected nodes. A weight is applied to each edge, the weight being a measure  
of the level of communication between the connected edges. Terminal nodes  
representative of the multiple computers are attached to the communication graph. Then,  
dominant edges are identified within the communication graph. For any non-terminal  
15 node, a connected edge is dominant if it is at least as heavy (its weight is greater than or  
equal to) as the sum of the remaining non-terminal edges and the heaviest of the remaining  
terminal edges. The min cut for the communication graph need not include any dominant  
edges and so, dominant edges are removed from consideration for the final min cut  
solution. Finally, program components which may be a single program unit or an  
20 aggregate of units are placed on computers according to the communication graph min cut  
solution.



100

**FIG. 1**

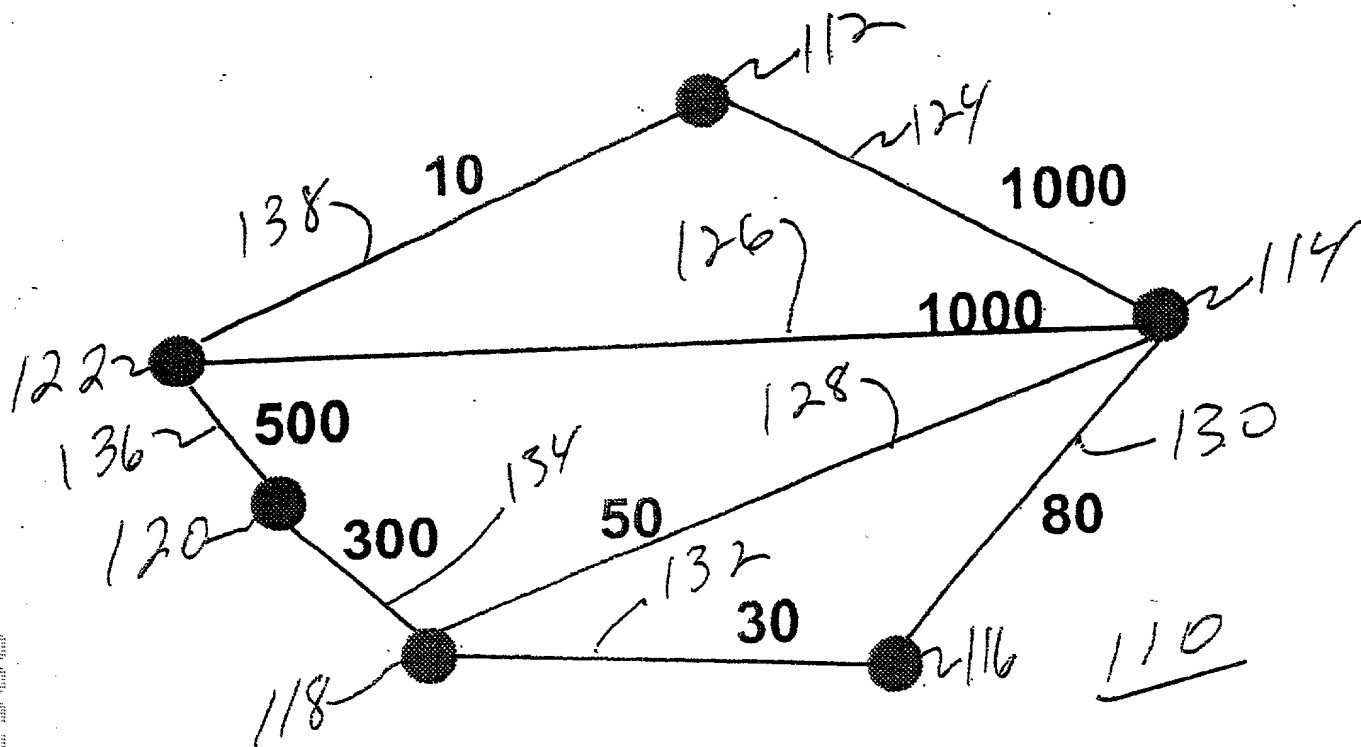


Fig. A

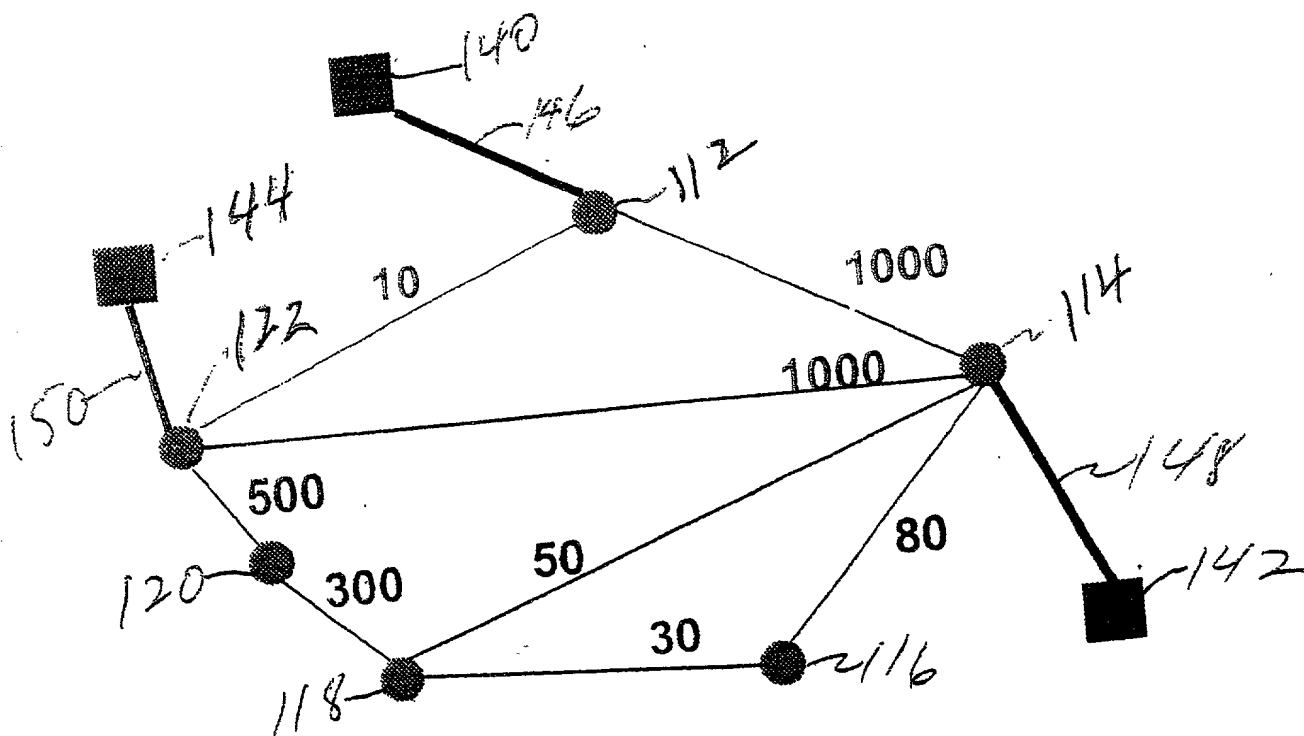
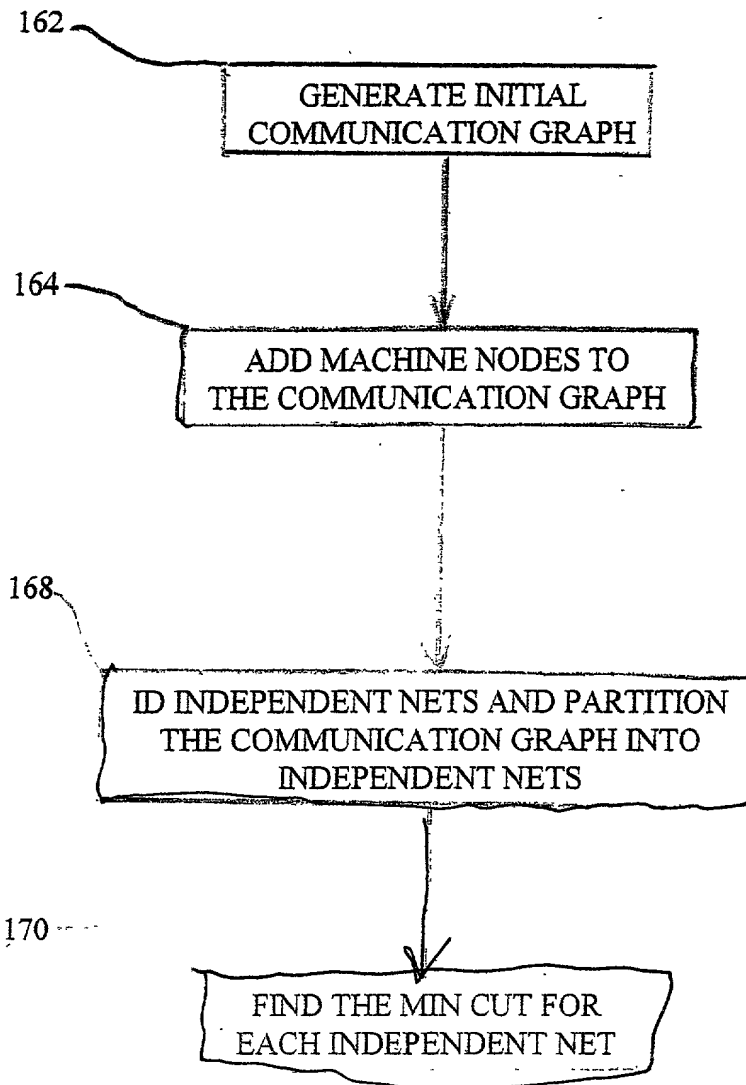


Fig. 2B







**FIG. 3**

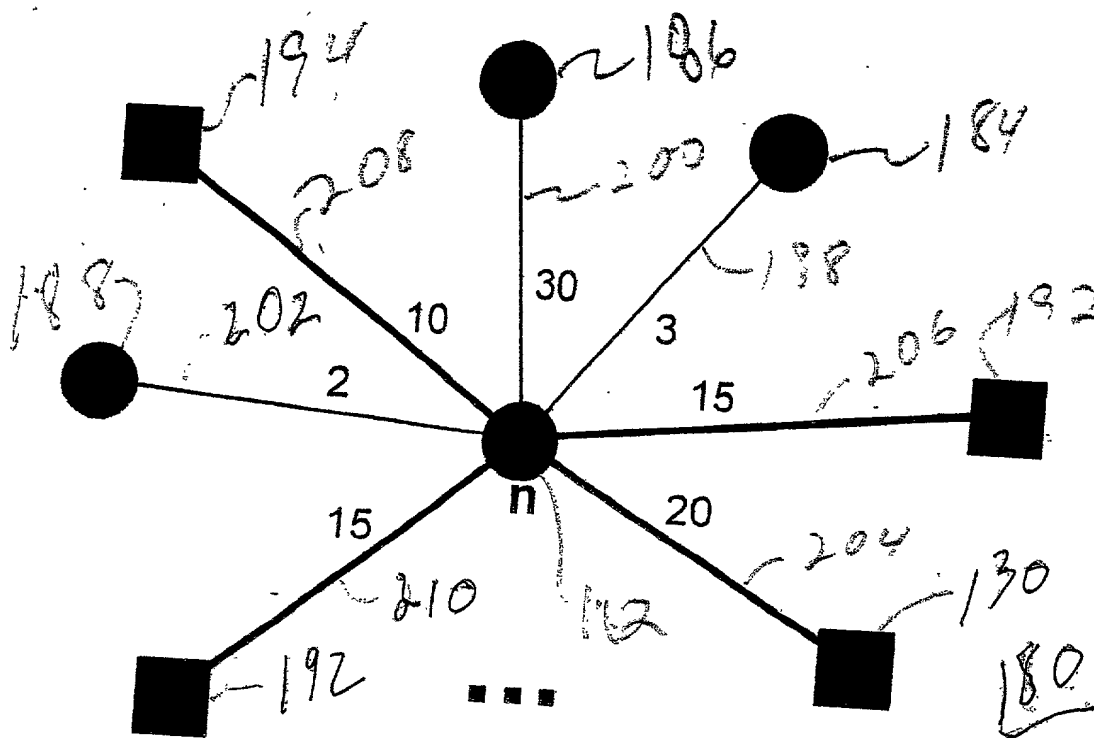


Fig 4

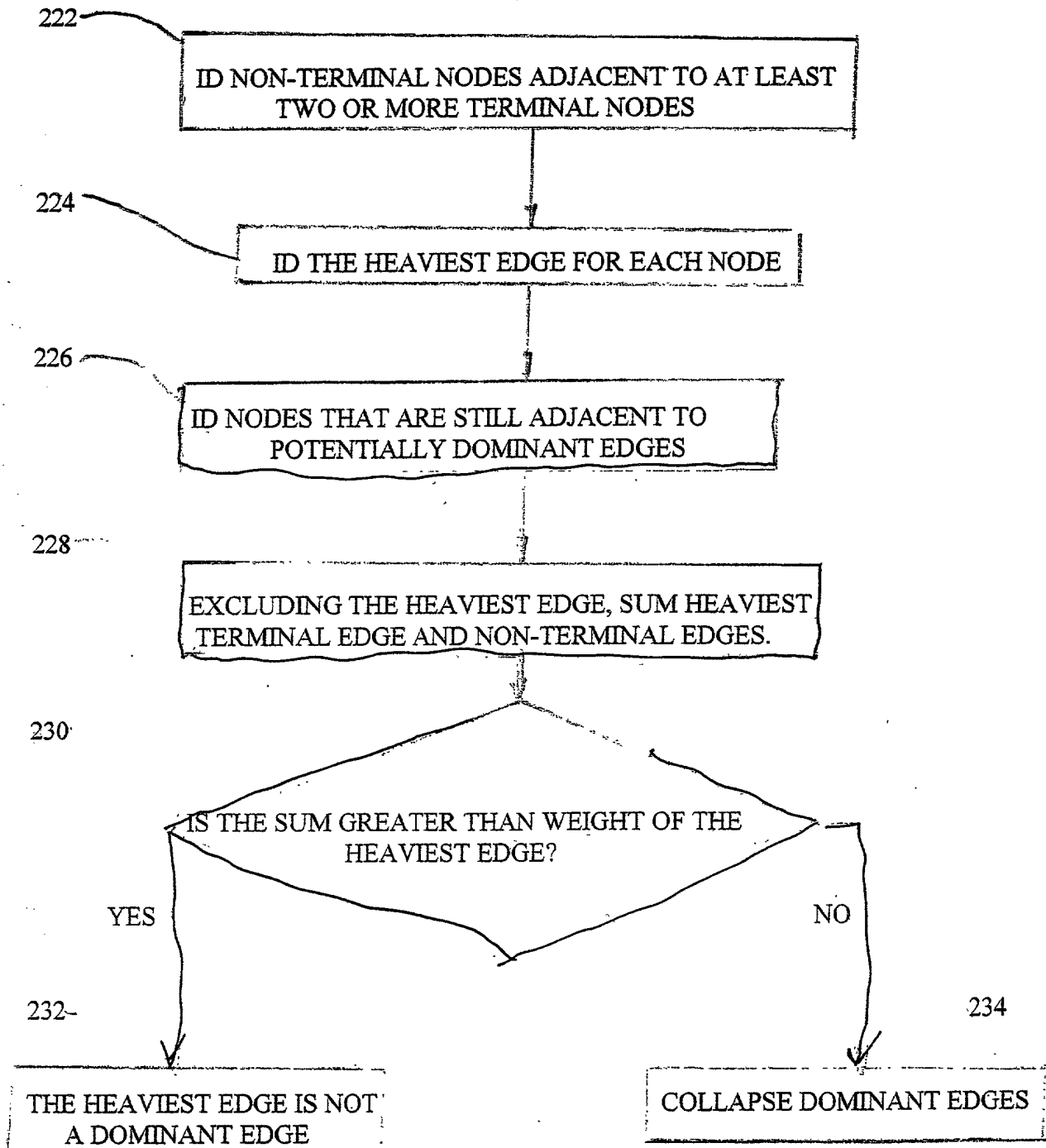
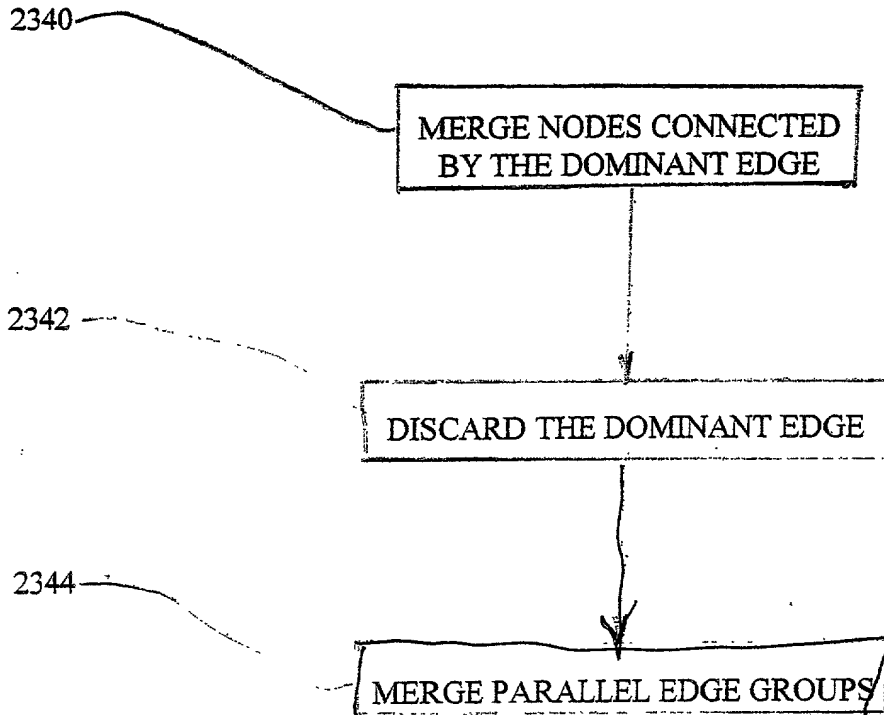


Fig. 5



**Fig. 6**

**DECLARATION AND POWER OF ATTORNEY FOR PATENT APPLICATION**

As a below named inventor, I hereby declare that:

My residence, post office address and citizenship are as stated below next to my name;

I believe I am the original, first and sole inventor (if only one name is listed below) or an original, first and joint inventor (if plural names are listed below) of the subject matter which is claimed and for which a patent is sought on the invention entitled:

**DOMINANT EDGE IDENTIFICATION FOR EFFICIENT PARTITION AND DISTRIBUTION**

the specification of which (check one)

☒ is attached hereto.

\_\_\_\_\_ was filed on \_\_\_\_\_ as United States Application Number

or PCT International Application Number \_\_\_\_\_

and was amended on \_\_\_\_\_ (if applicable)

I hereby state that I have reviewed and understand the contents of the above identified specification, including the claims, as amended by any amendment referred to above.

I acknowledge the duty to disclose information which is material to the patentability of this application in accordance with Title 37, Code of Federal Regulations, Section 1.56.

I hereby claim foreign priority benefits under Title 35, United States Code, §119(a)-(d) or §365(b) of any foreign application(s) for patent or inventor's certificate, or §365(a) of any PCT International application which designated at least one country other than the United States, listed below and have also identified below, by checking the box, any foreign application for patent or inventor's certificate, or PCT International application, having a filing date before that of the application on which priority is claimed:

Prior Foreign Application(s)	Priority Claimed
(Number) _____ (Country) _____ (Day/Month/Year Filed) _____	<input type="checkbox"/> Yes <input type="checkbox"/> No
(Number) _____ (Country) _____ (Day/Month/Year Filed) _____	<input type="checkbox"/> Yes <input type="checkbox"/> No
(Number) _____ (Country) _____ (Day/Month/Year Filed) _____	<input type="checkbox"/> Yes <input type="checkbox"/> No

I hereby claim the benefit under 35 U.S.C. §119(e) of any United States provisional application(s) listed below.

(Application Number) \_\_\_\_\_ (Filing Date) \_\_\_\_\_

(Application Number) \_\_\_\_\_ (Filing Date) \_\_\_\_\_

I hereby claim the benefit under 35 U.S.C. §120 of any United States Application(s), or §365(c) of any PCT International application designating the United States, listed below and, insofar as the subject matter of each of the claims of this application is not disclosed in the prior United States, or PCT International application in the manner provided by the first paragraph of 35 U.S.C. §112, I acknowledge the duty to disclose information material to the patentability of this application as defined in 37 CFR §1.56 which occurred between the filing date of the prior application and the national or PCT international filing date of this application:

(Application Serial No.) _____	(Filing Date) _____	(Status) (patented, pending, abandoned) _____
(Application Serial No.) _____	(Filing Date) _____	(Status) (patented, pending, abandoned) _____

I hereby declare that all statements made herein of my own knowledge are true and that all statements made on information and belief are believed to be true; and further that these statements were made with the knowledge that willful false statements and the like so made are punishable by fine or imprisonment, or both, under Section 1001 of Title 18 of the United States Code and that willful false statements may jeopardize the validity of the application or any patent issued thereon.

POWER OF ATTORNEY: As a named inventor I hereby appoint the following attorney(s) and/or agent(s) to prosecute this application and transact all business in the Patent and Trademark Office connected therewith (list name and registration number).

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